

## Generative Design

- physical
- computational

## Design Optimization

- physical
- computational

## Parametric Design

- scalar
- repetitive / modular
- algorithmic

## Genetic Design

- search
- optimization
- exploration



## Optimization

### What to optimize (levels)

- material
- member
- geometry
- topology

### How to optimize (methods)

- physical
- computational

# Optimization

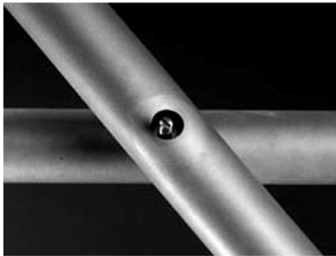
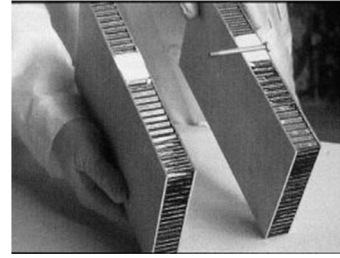
Material  
Member  
Geometry  
Topology

Minimize

Weight  
Volume  
Cost

Maximize

Strength  
Strain Energy  
Elasticity  
Ductility  
Stiffness



# Optimization

Material  
Member  
Geometry  
Topology

Strength (Full Utilization)

in section  
in length

Stability (no buckling)

in section  
in length

Serviceability

in use  
maintenance

Connections

stress transfer



# Optimization

Material

Member

Geometry

Topology

Arrangement of Nodes

best overall for members

includes optimization of :

- material
- members



Truss: 1 weight = 27246 lb  
16 joints 31 members



Truss: 2 weight = 23083 lb  
16 joints 31 members



Truss: 3 weight = 22836 lb  
16 joints 31 members

# Optimization

Material

Member

Geometry

Topology

Arrangement of Members

includes optimization of :

- material
- members
- geometry



Truss: 1 weight = 25484 lb  
16 joints 35 members



Truss: 2 weight = 25050 lb  
16 joints 35 members

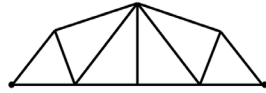


Truss: 3 weight = 24529 lb  
16 joints 35 members

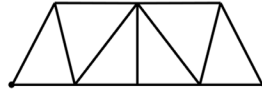
# Geometry vs. Topology

## definitions

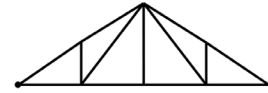
Three Examples of Geometry:



Topo ID: 1  
jnt 8 mbr 13

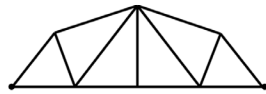


Topo ID: 1  
jnt 8 mbr 13

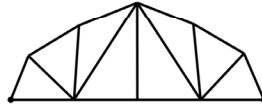


Topo ID: 1  
jnt 8 mbr 13

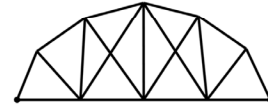
Three Examples of Topology:



Topo ID: 1  
jnt 8 mbr 13



Topo ID: 2  
jnt 10 mbr 17



Topo ID: 3  
jnt 10 mbr 19

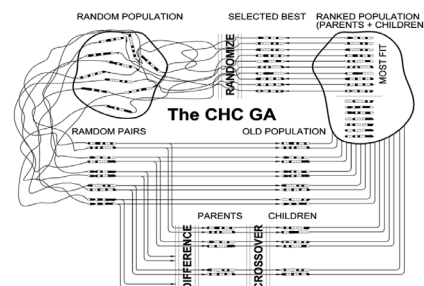
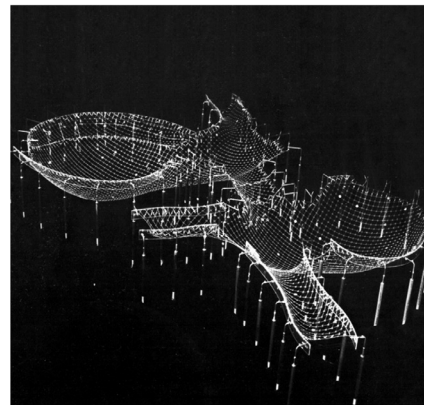
## Methods

### Physical

- structural models
- form finding models
- analog models

### Computational

- Linear Programming (Simplex)
- Homogenous – sensitivity
- Stochastic/Probabilistic Algorithms
  - GA (Genetic Algorithms)
  - ES (Evolutionary Strategies)
  - SA (Simulated Annealing)
  - Swarming (Particle Swarm Optimization)





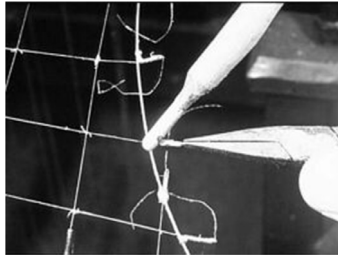
# Methods

## Physical

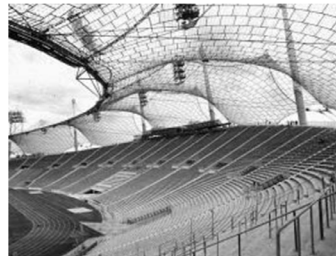
- structural models
- form finding models
- analog models



Louis I. Kahn's structural model for the Richards Medical Research Laboratory



Frei Otto's model of the cable nets of the 1972 Olympics



Stadium in Munich from 1972 Olympics

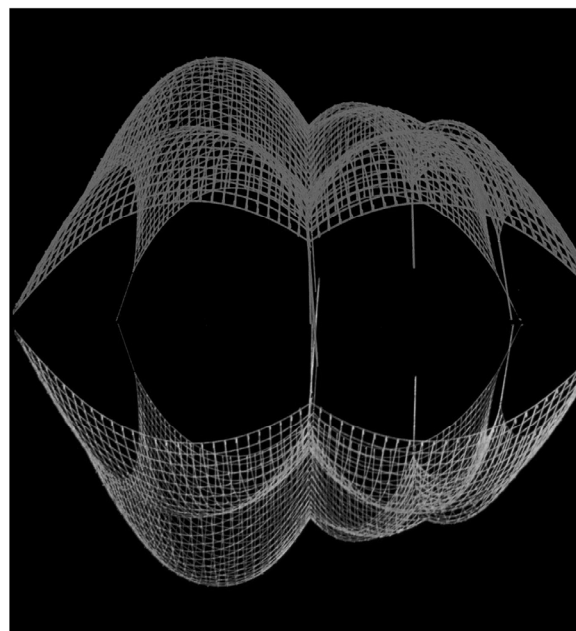
# Methods

## Physical

- structural models
- form finding models
- analog models



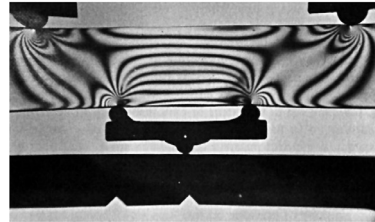
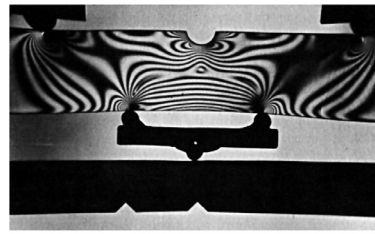
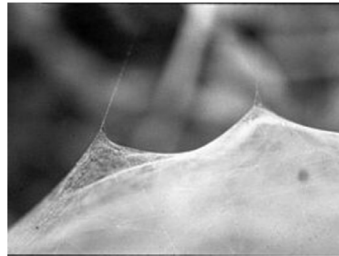
Heinz Isler, Burgdorf



# Methods

## Physical

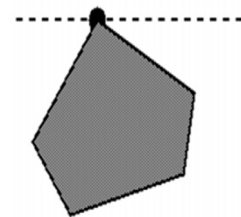
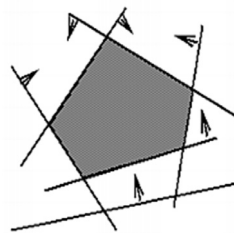
- structural models
- form finding models
- analog models



# Methods

## Computational

- Linear Programming (Simplex)
- Homogenous – sensitivity
- Evolutionary Algorithms
  - ES (Evolutionary Strategies)
  - GA (Genetic Algorithms)



# Methods

Computational

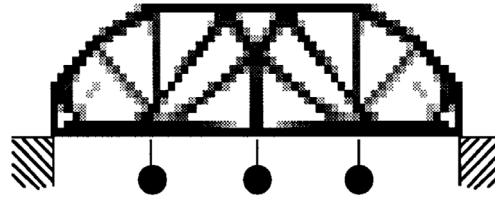
Linear Programming (Simplex)

Homogenous – sensitivity

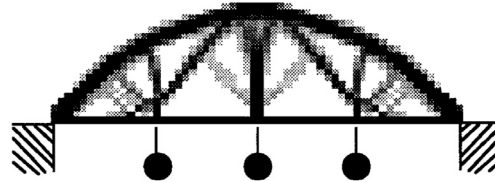
Evolutionary Algorithms

ES (Evolutionary Strategies)

GA (Genetic Algorithms)



(a) Design I



(b) Design II

# Methods

Computational

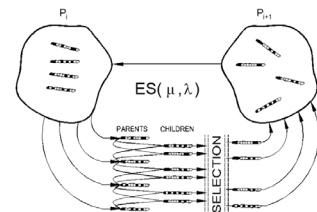
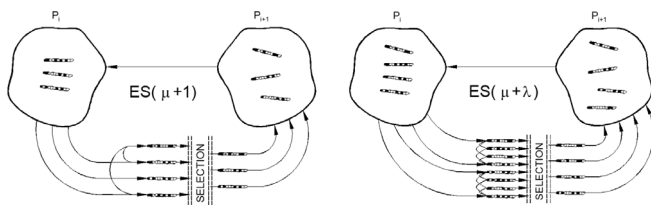
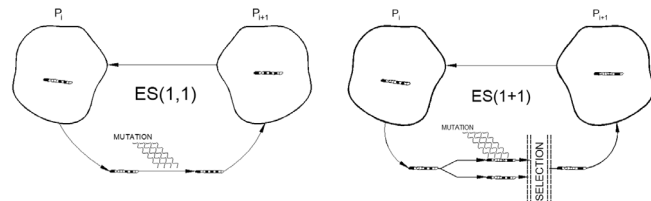
Linear Programming (Simplex)

Homogenous – sensitivity

Evolutionary Algorithms

ES (Evolutionary Strategies)  
Rechenberg & Schwefel

GA (Genetic Algorithms)  
John Holland



- (1, 1) random walk
  - (1+1) one parent → one child - select from all
  - (μ+1) multi-parent → one child - select from all
  - (μ+λ) multi-parent → multi-child - select from all
  - (μ, λ) multi-parent → multi-child - select from children
- (Bäck, 1996)

# Methods

## Computational

Linear Programming (Simplex)

Homogenous – sensitivity

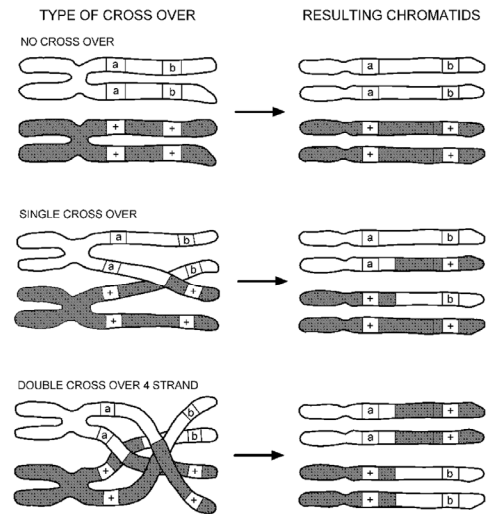
Evolutionary Algorithms

ES (Evolutionary Strategies)

GA (Genetic Algorithms)

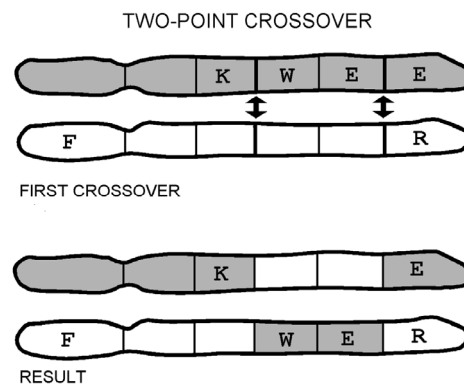
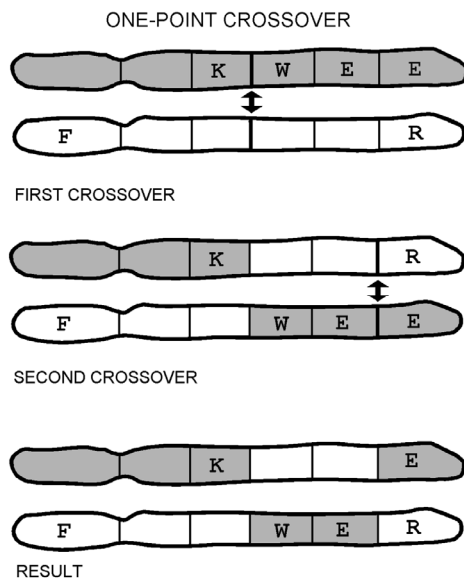
Selectorecombinative

- selection
- crossover
- mutation



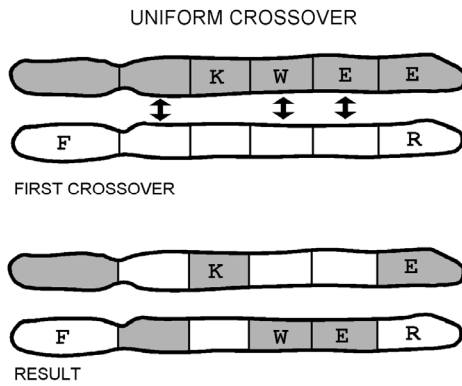
# Genetic Algorithms

## crossover

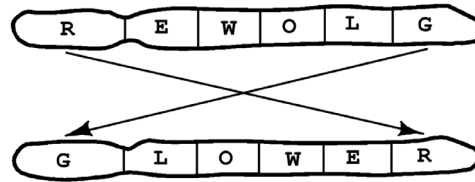


# Genetic Algorithms

## crossover

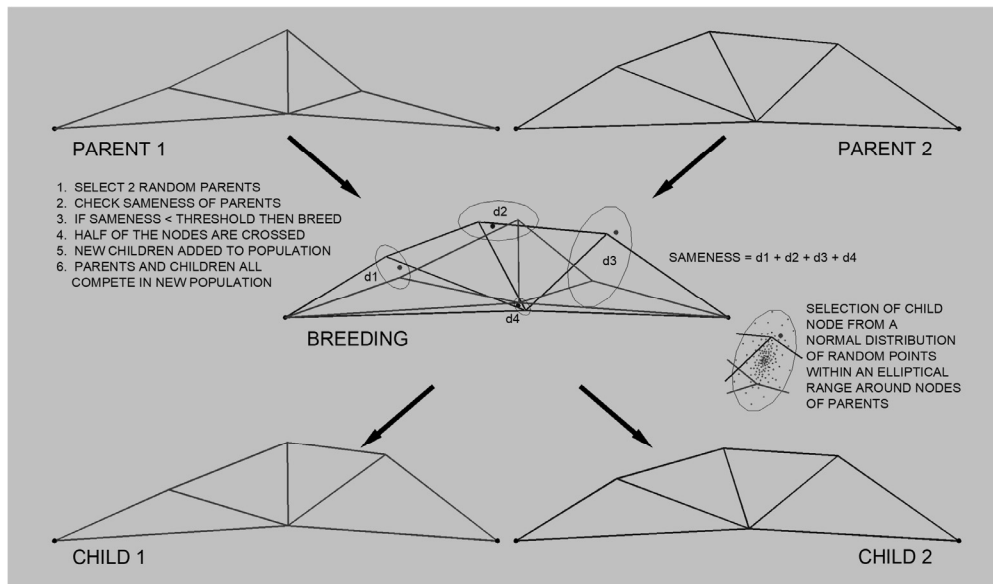


## inversion



# Genetic Algorithms - Geometry

## half-uniform crossover



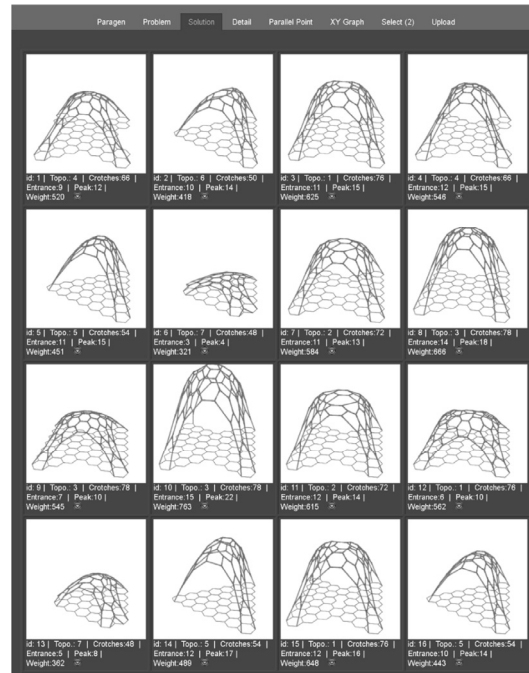
# Genetically Enhanced Parametric Design for Performance Optimization and Design Exploration

## The ParaGen Method

Form Exploration in Early Design Phases

Based on Parametric Geometry, GA search with a SQL database

Peter von Buelow, Dr. –Ing.  
Professor in Architecture  
University of Michigan



## Aspects of Early Design

### Purposeful

directed – not merely random

### Goal Oriented

search to find good solution

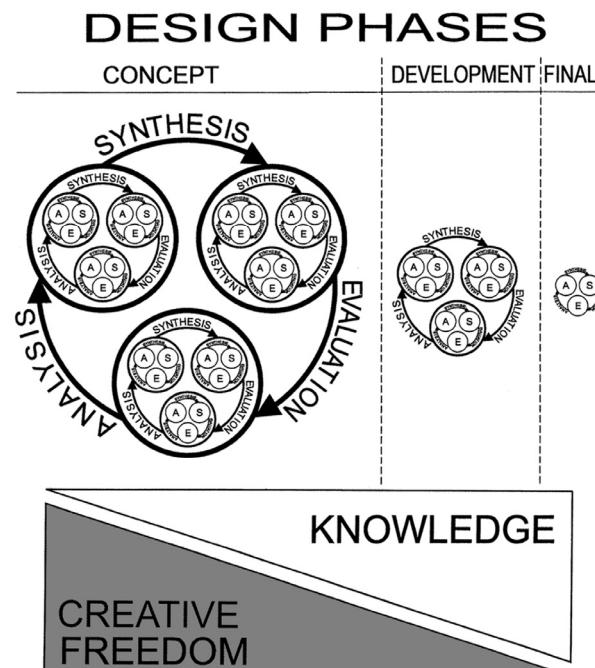
### Creative

seeks new solutions

### Ill Structured Problems

problem space not fully defined  
cannot solve directly – cyclic

exploration is needed



# Exploration with Evolutionary Computation

deterministic optimization  
focuses on one 'best' solution

It is better suited for later  
design phases

exploration tries to expose a  
range of 'pretty good' solutions

it aids ideation and creativity in  
early design phases



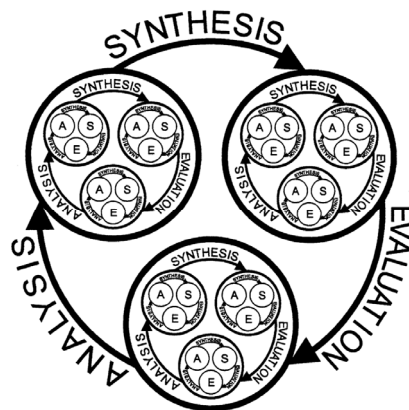
## Why GA's fit well to early design

### Early Design

- Explorative
- Recursive
- Serendipitous
- Knowledge of design is low

### GA Design

- Populations of solutions
- Operates in cycles
- Random mutations
- No knowledge of fitness function



# The ParaGen Exploration Method

Based on an NDDP-GA

## Oriented toward Exploration

- Helps designer understand the range of solutions

## Non-Destructive

- All solutions are visible

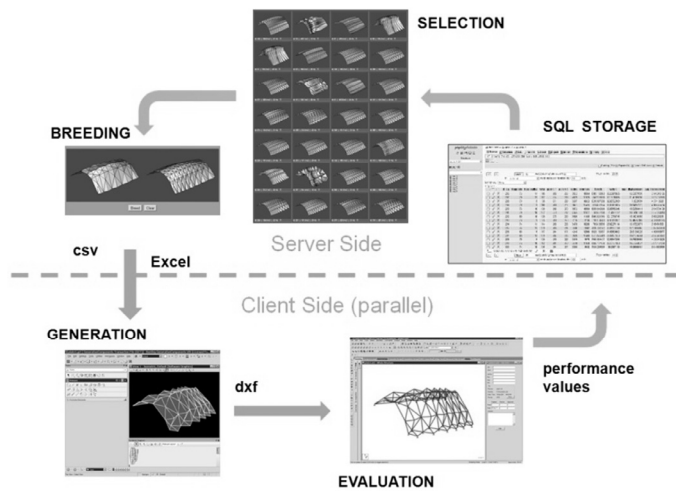
## Dynamic Populations

- Well suited for multi-objectives

## Both Interactive and Algorithmic

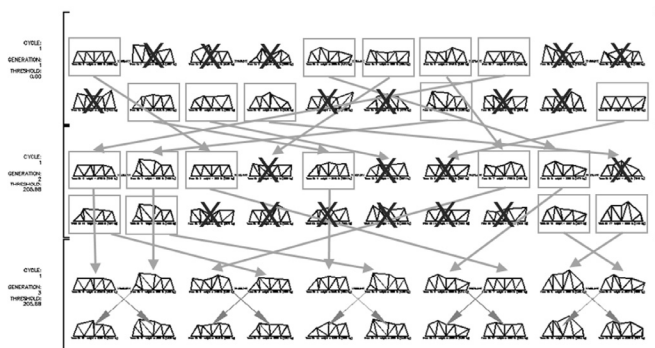
- Can consider non-computational criteria, e.g. aesthetics

## The ParaGen Framework

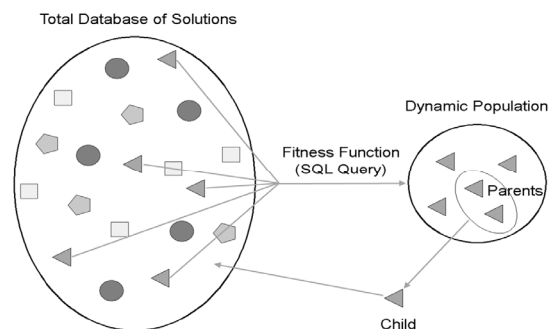


## ParaGen is Non-Destructive

Traditional GAs are destructive – solutions are lost



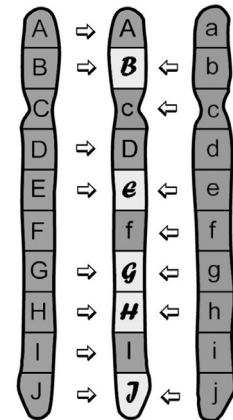
An NDDP-GA is non-destructive  
no solutions are lost





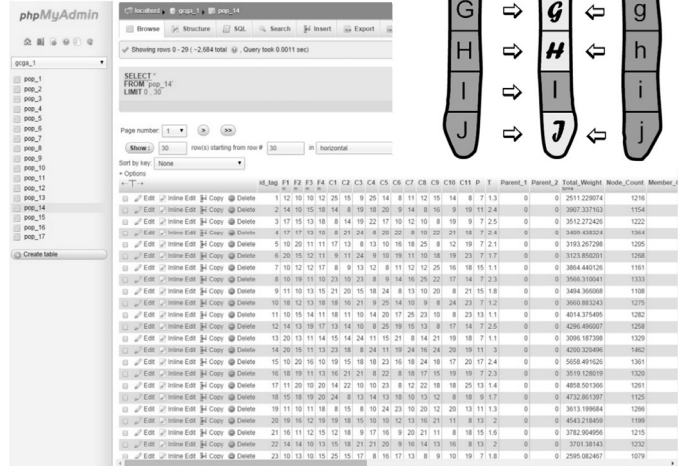
# GA + SQL = Exploration

Parent 1    Child    Parent 2



## Seven Points:

1. Store no duplicates
2. Multi-objective
3. Dynamic populations
4. Changeable search direction - corrective
5. Interactive search
6. Pareto optimization
7. Parallel computation



# 1. Store All Solutions without Duplicates

## Relational Database Size

- terabyte range (e.g. 256 TB in MySQL, but limited by system)

## SQL unique index

- set at child generation
- checked at data entry

## Faster analysis

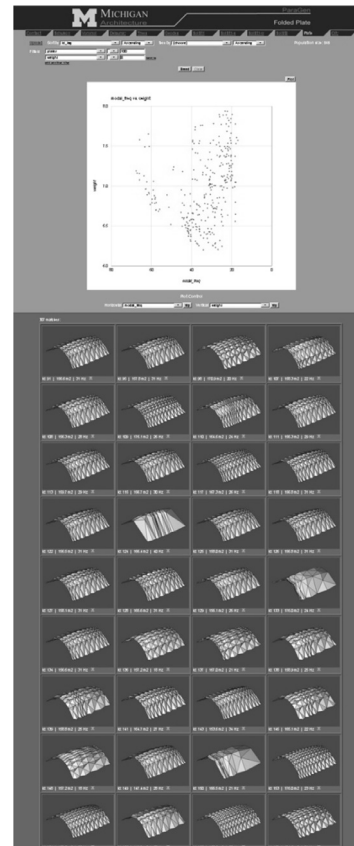
- no duplicate solutions to analyze

## More effective post analysis

- no duplicate solutions to view
- more descriptive graphing

## Less storage space needed

- only unique solutions are retained

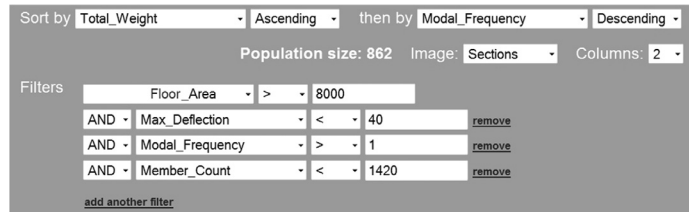


## 2. Use Multi-Objective Fitness Functions

### Fitness defined by SQL query

- simple sorts – single variable  
e.g. 20 best
- defined range – single variable  
e.g. between max. and min.
- Multi-objective query  
e.g. Pareto set optimization  
e.g.

*weight* less than x AND  
*height* more than y AND  
*heat gain* less than z



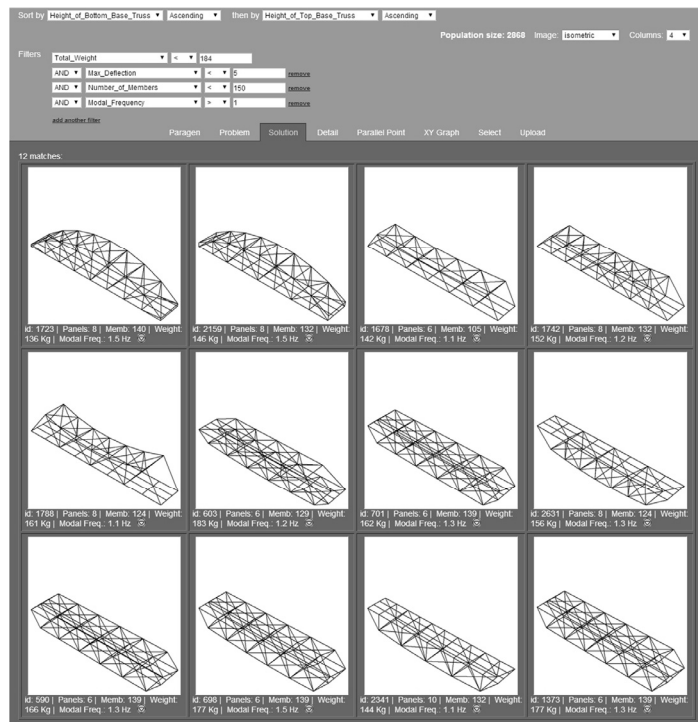
### Separate fitness for each parent

- each parent can be obtained  
using a different query set

## 3. Create Dynamic Parent Populations

### Independent breeding population

- Not dependent on  
previous population
- Non-generational or  
static population
- Evolution through  
addition (no loss)



## 4. Change Search Direction

### Search different parts of solution space

- see range of solutions
- bracket uncertainty
- conflicting design desires

### Change fitness without restarting

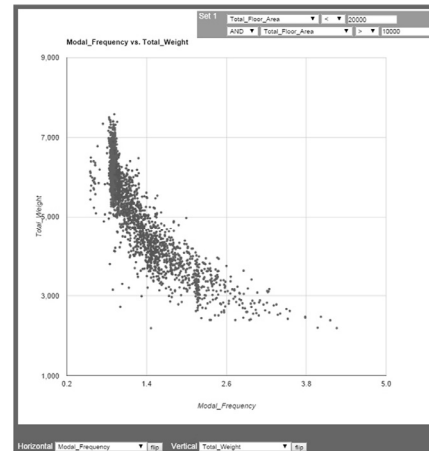
- changing the fitness criteria merely shifts the view

### Aids in post analysis

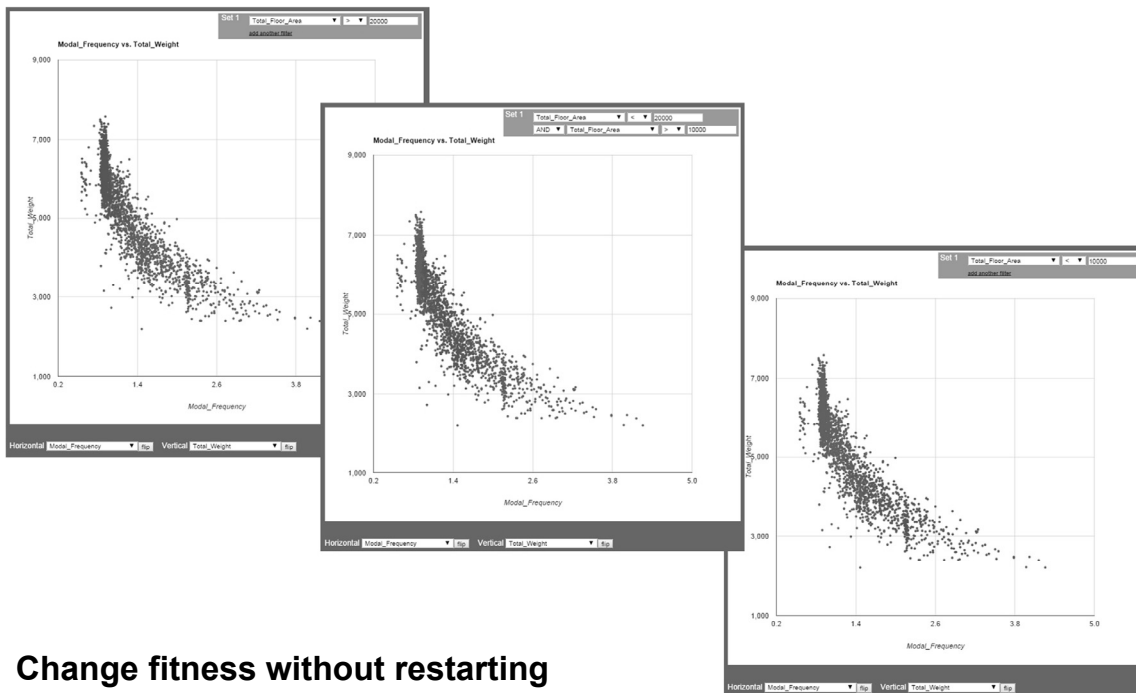
- allows for the comparison of conflicting solutions

### Allows correction of objectives

- objectives can be easily refined as more data is made available



### Search different parts of solution space



### Change fitness without restarting

# 5. Interactive Exploration of Solutions

## No delay for analysis

- near immediate response to queries

## Variety of graphic depiction

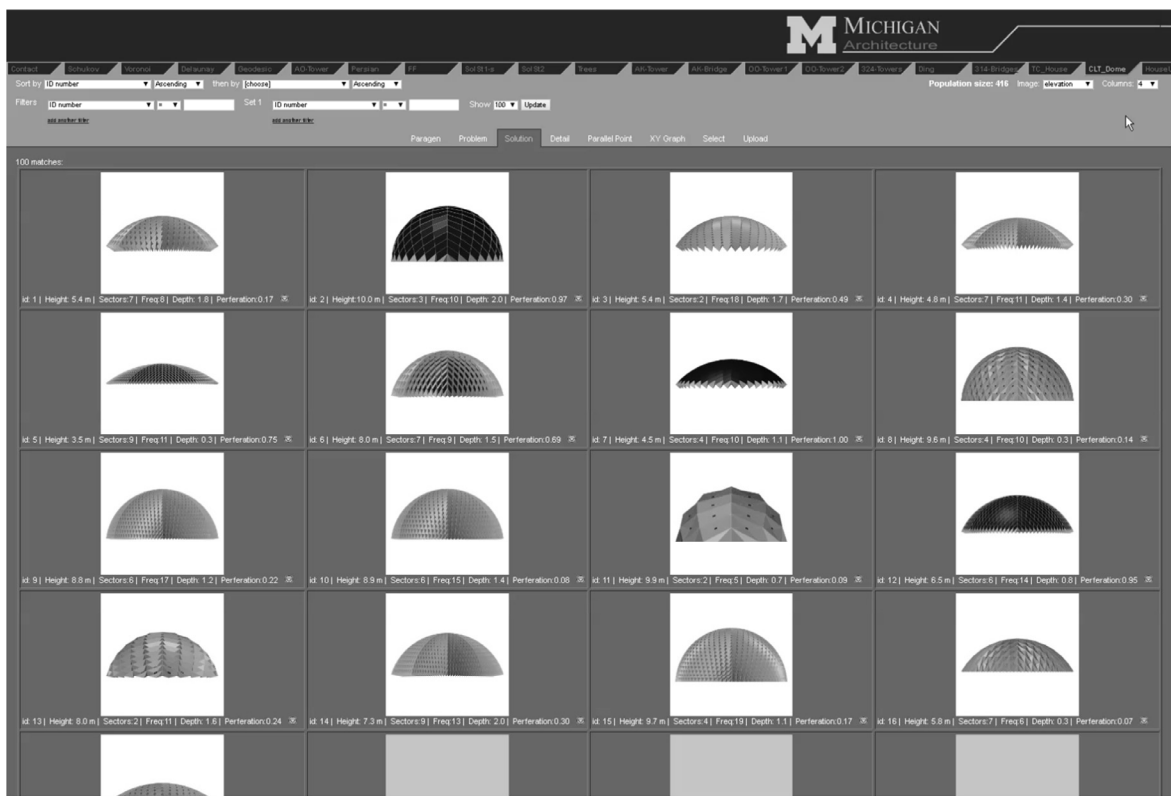
- multiple image views (different information)
- control visual array display



## Aids in post analysis

- allows for the comparison of conflicting solutions

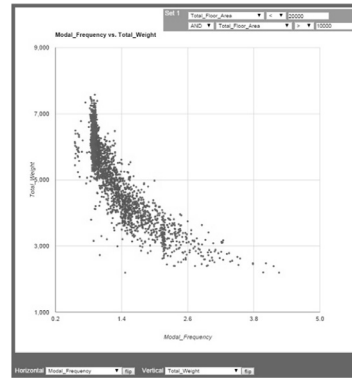
# Control visual array display



## 6. Versatile Graphing Data Analysis

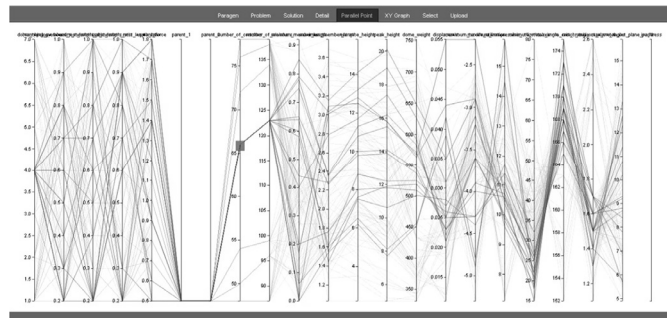
### x-y scatter graphs

- filters to set range of points
- plot any two variables or values
- control axis direction
- Show third parameter with color

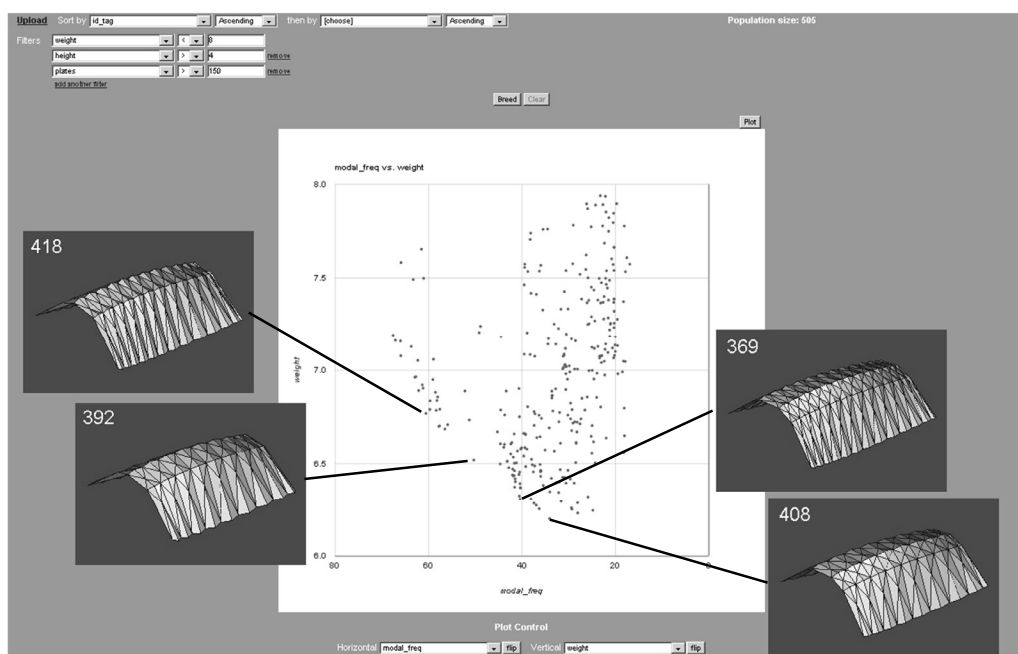


### parallel coordinate graphs

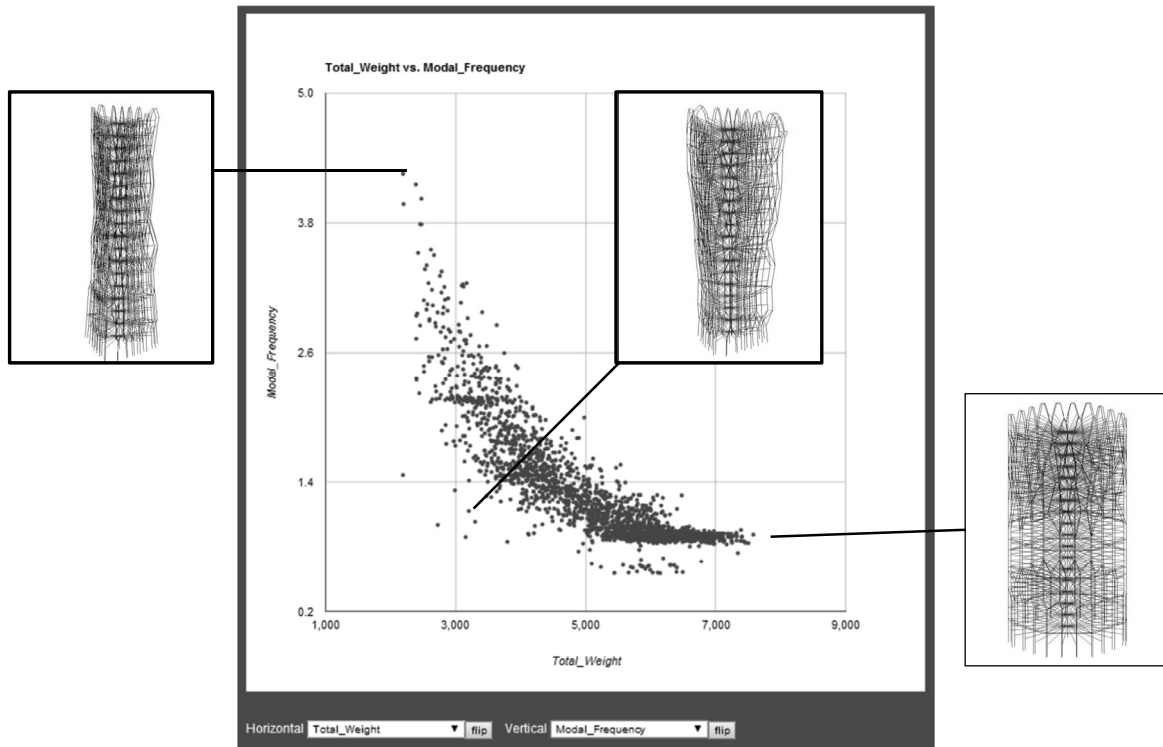
- filters to set range of points
- highlight any set (box select)



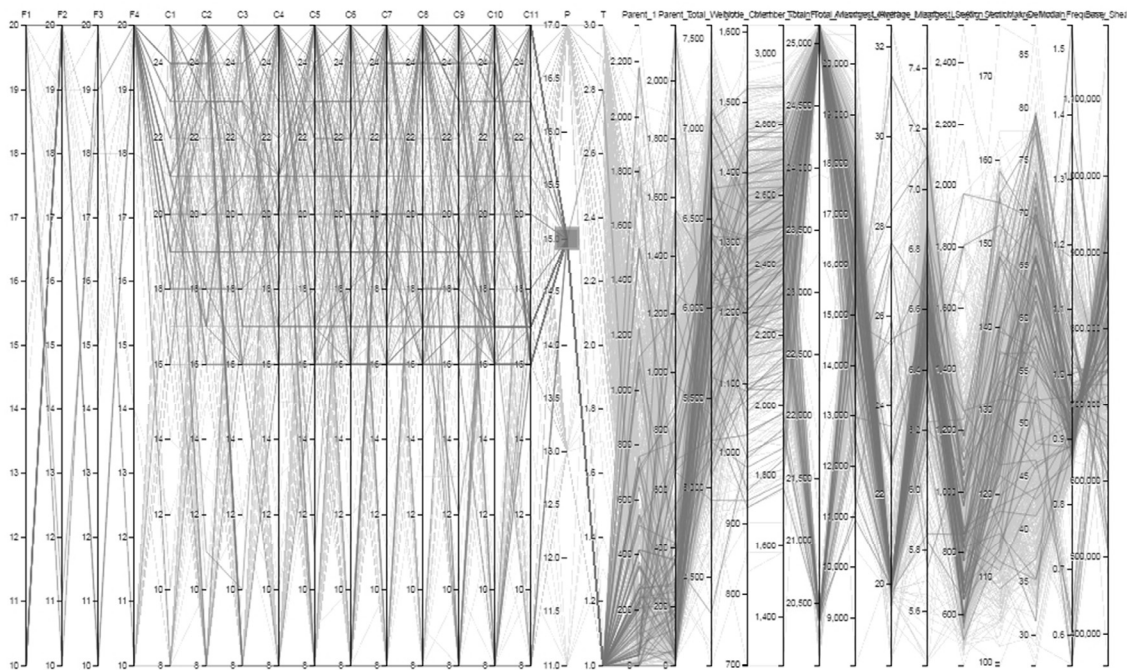
## x-y scatter graphs



# x-y scatter graphs



# parallel coordinate graphs



# Pareto optimization

Define conflicting objectives

e.g.  
weight and stiffness

Determine non-dominated solutions

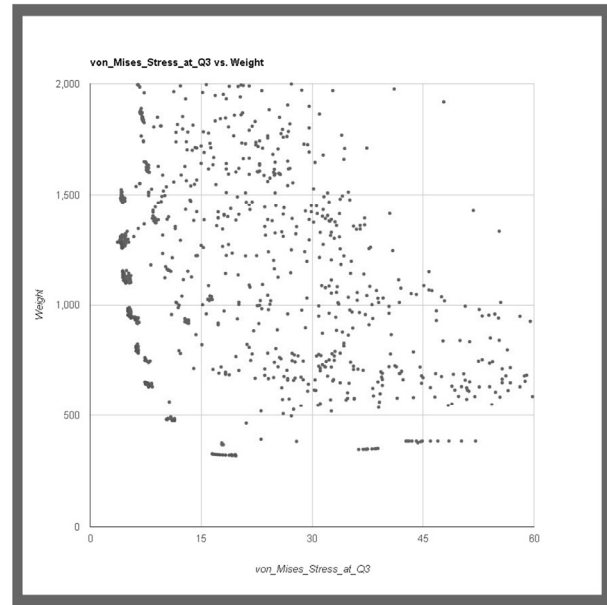
e.g.  
For a given solution there is  
no lower weight with a higher  
stiffness

Define the Pareto set of non-dominated  
solutions

Sort and breed neighbors

or

Select and mutate individuals

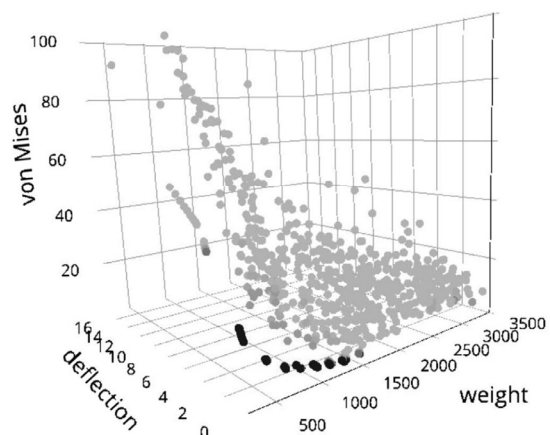


# Pareto optimization

Selection can contain any number of  
objectives

e.g.  
weight and deflection and stress

weight vs. deflection vs. von Mises stress



# 7. Utilize Parallel Hardware

Dedicated cluster (cloud)

or

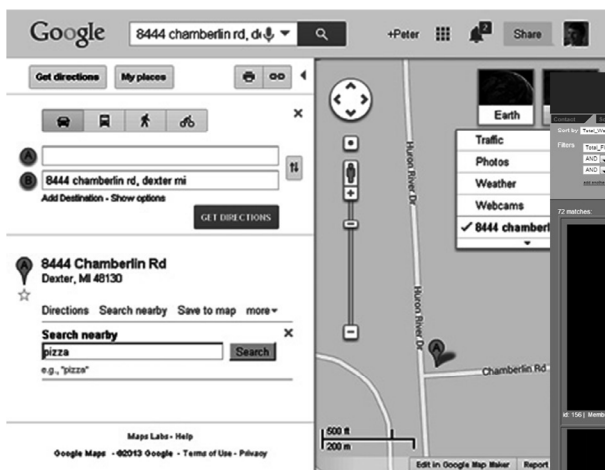
ad hoc cluster

- Simple web browser connection

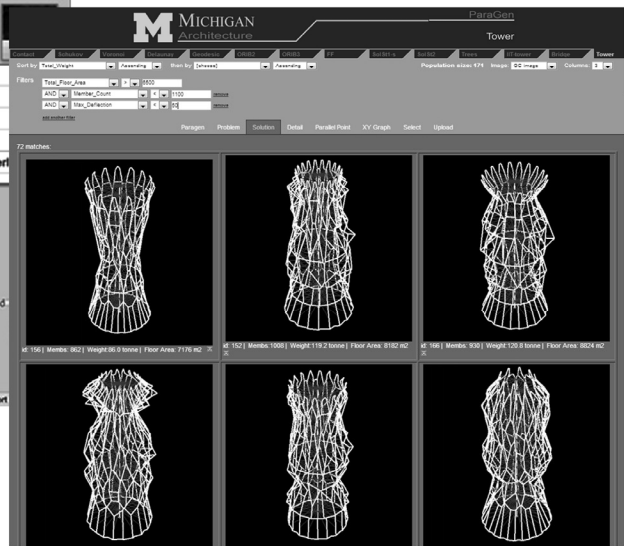


# Exploration as Database Mining

Google maps



ParaGen maps



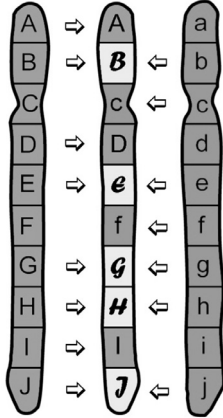




## 2. Breeding

- Create population from data
- Crossover of data variables
- Half Uniform Crossover
- Output to Excel

Parent 1    Child    Parent 2



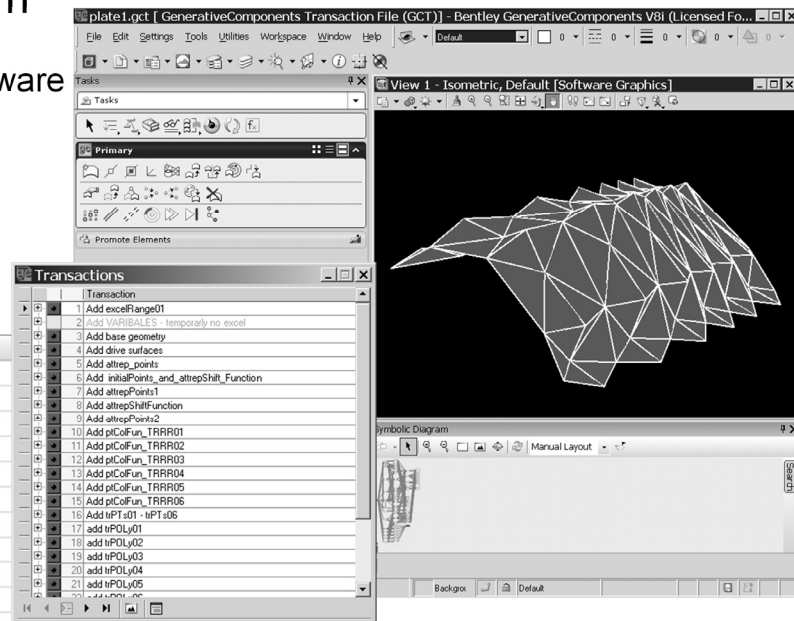
HUX

SQL database

## 3. Grow the Form

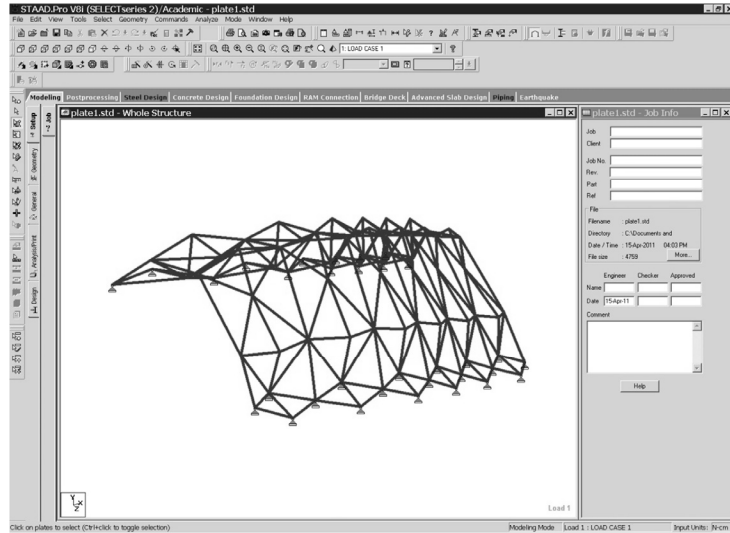
- Run parametric software with Excel input.
- Generate form.
- Output dxf file.
- Capture image.

	A	B
1	U_LATITUDE_NUMBER	0.3
2	V_LONGITUDE_NUMBER	0.3
3	OFFSET_CREST	0.2
4	OFFSET_EDGE	0.5
5	SHIFT_POINT_1_U_MULT	0.6
6	SHIFT_POINT_1_V_MULT	0.7
7	SHIFT_POINT_2_U_MULT	0.2
8	SHIFT_POINT_2_V_MULT	0.4
9	SHIFT_POINT_1_U_LOCATE	0.8
10	SHIFT_POINT_1_V_LOCATE	0.1
11	SHIFT_POINT_2_U_LOCATE	0.7
12	SHIFT_POINT_2_V_LOCATE	0.9
13	p1	134
14	p2	243
15		



## 4. Evaluate Form

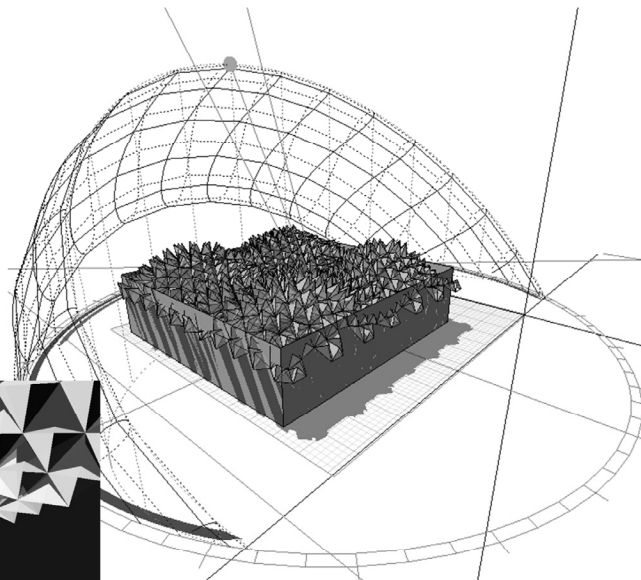
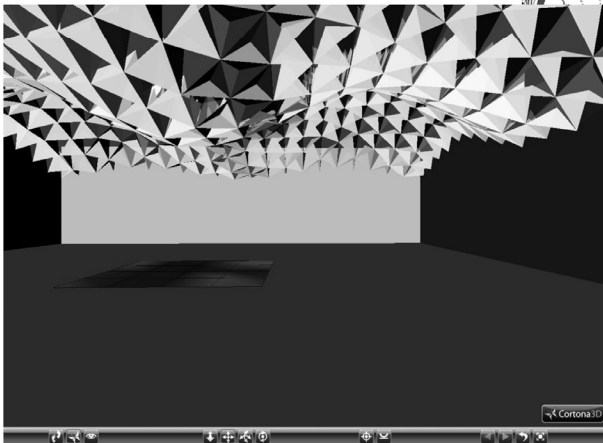
- Read into STAAD.Pro
- Add material, support and load conditions
- Find force and deflection
- Size members
- Determine weight
- Output data to Excel



## 4. Evaluate Form

Other performance evaluations can be made with any Windows software package.

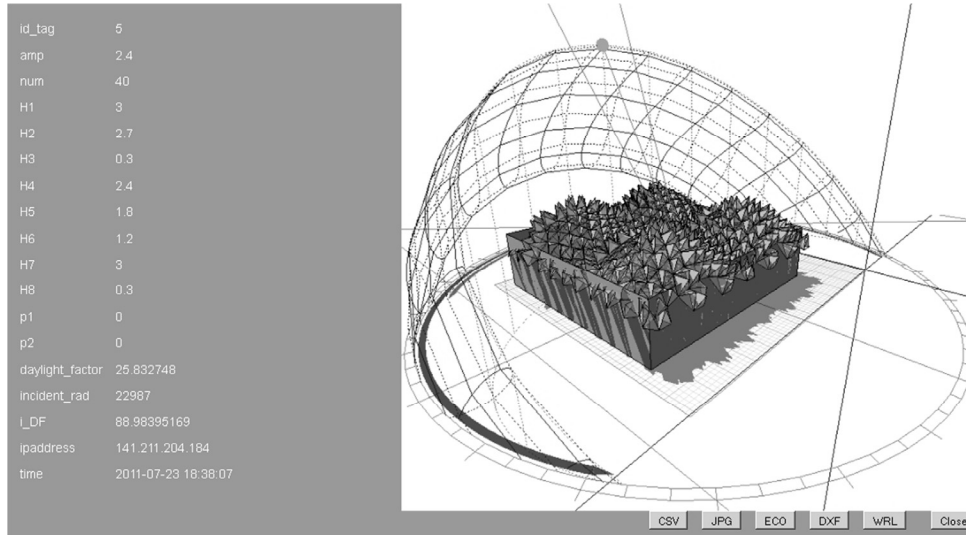
Example from Ecotect



## 5. Upload Files and Data to Web Server

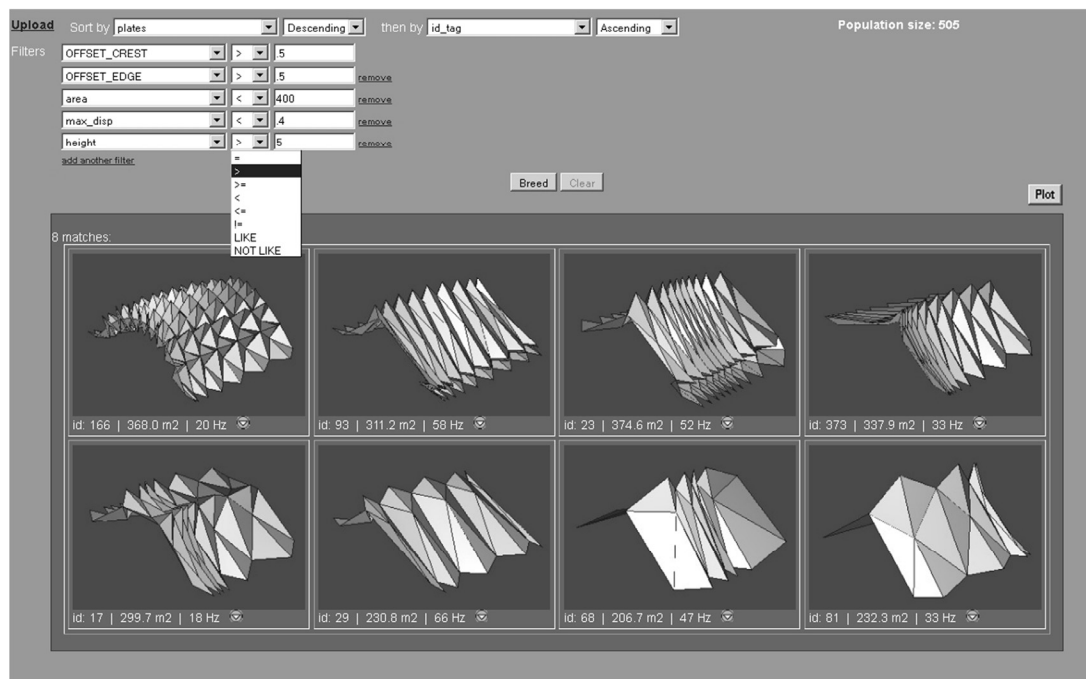
All variables and performance values are stored in a SQL database

Useful files are retained for later inspection: e.g. DXF, JPG, VRLM, and input files for FEA and Ecotect



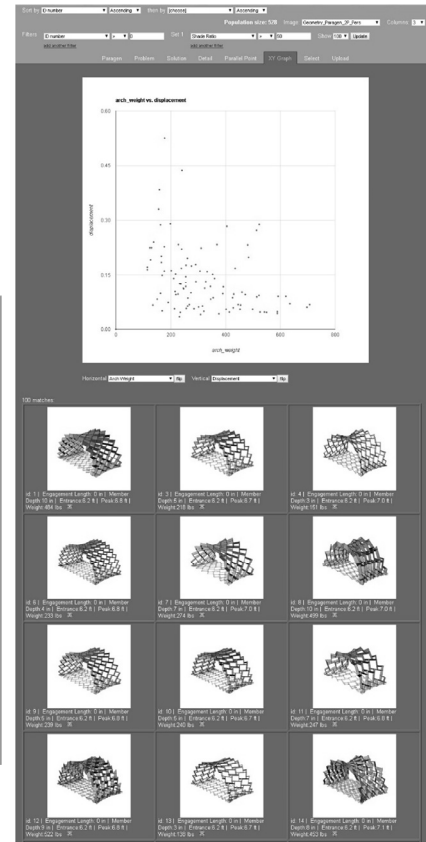
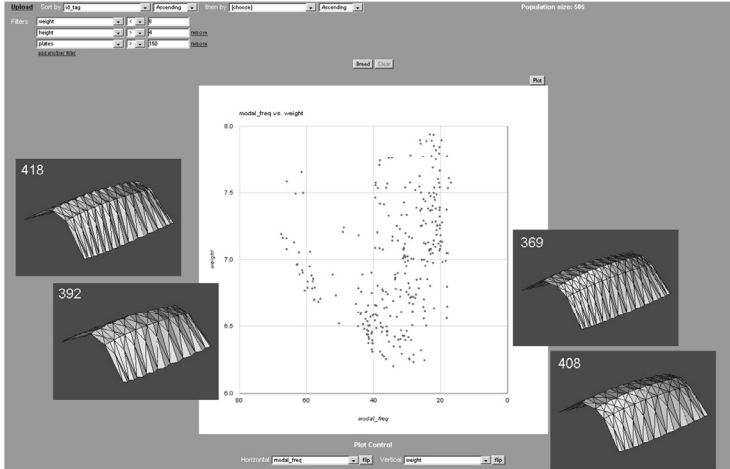
## 5. Store and Rank Data

Multi level sort options + multi level filters, together with image browsing of solutions provides robust exploration potential.

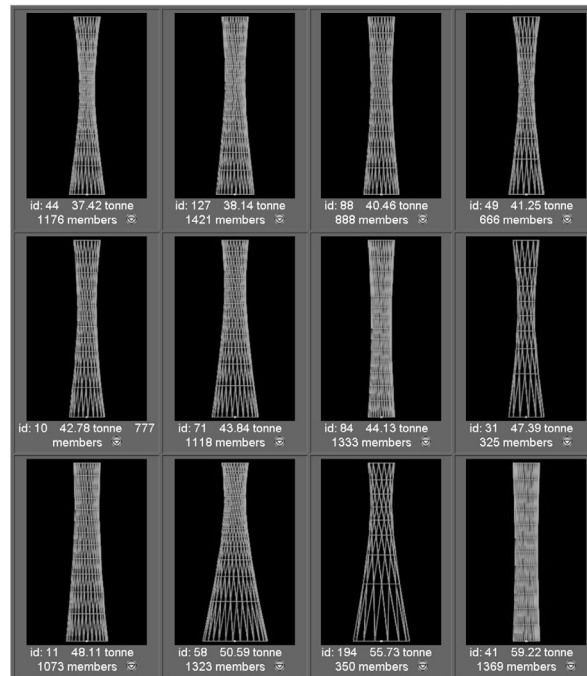
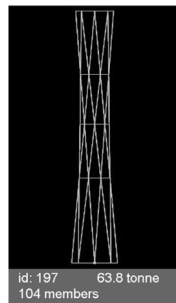
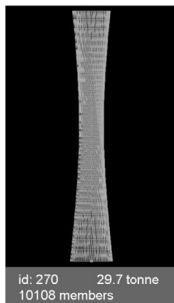
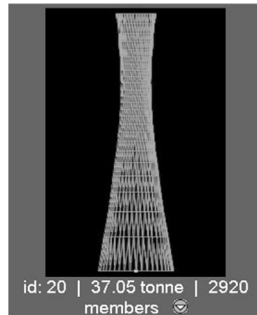


# How to use it

Post processing  
Exploration  
Selection



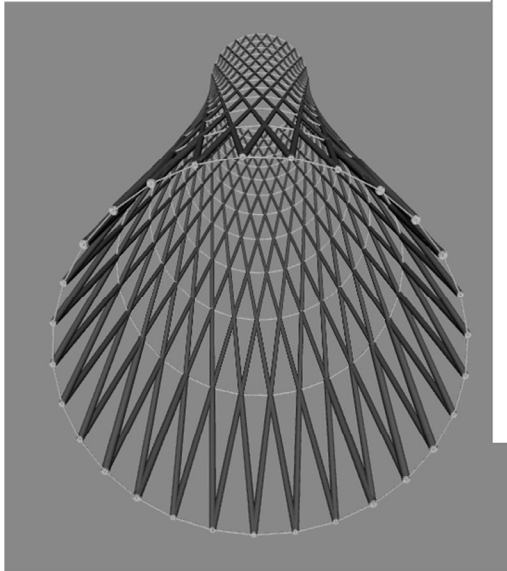
# Examples - Shukhov Tower



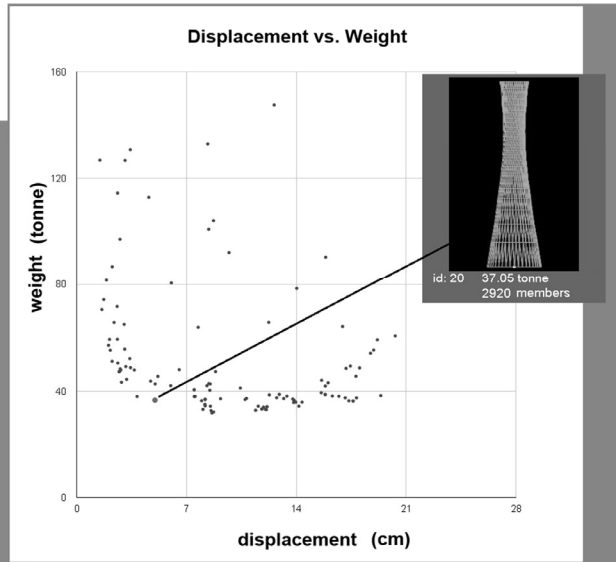
lightest weight least members

Dead + Wind Load

# Examples - Shukhov Tower

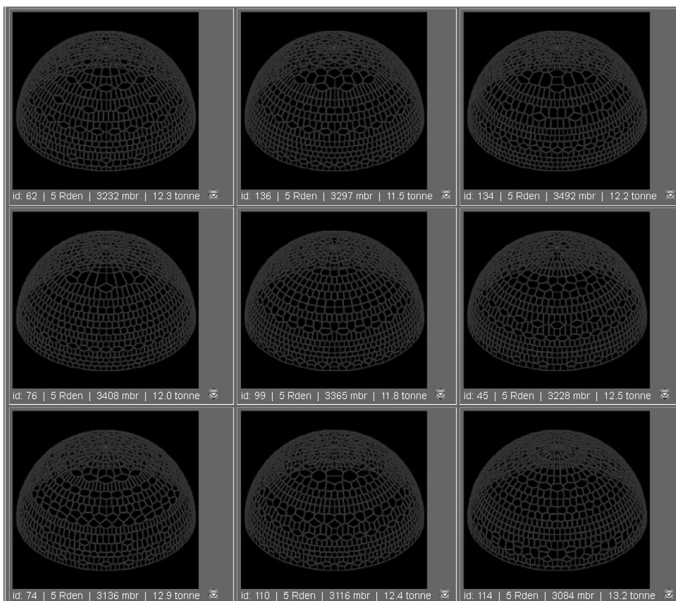


VRML perspective



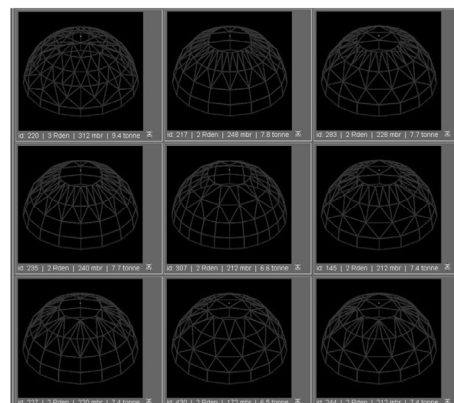
Plot of weight vs. members

## Examples (with Michela Turrin & Maria Van Embden Andres)

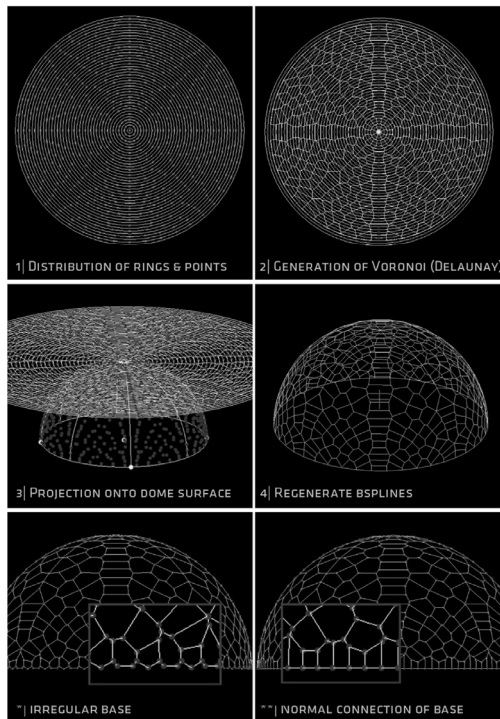


Voronoi Domes

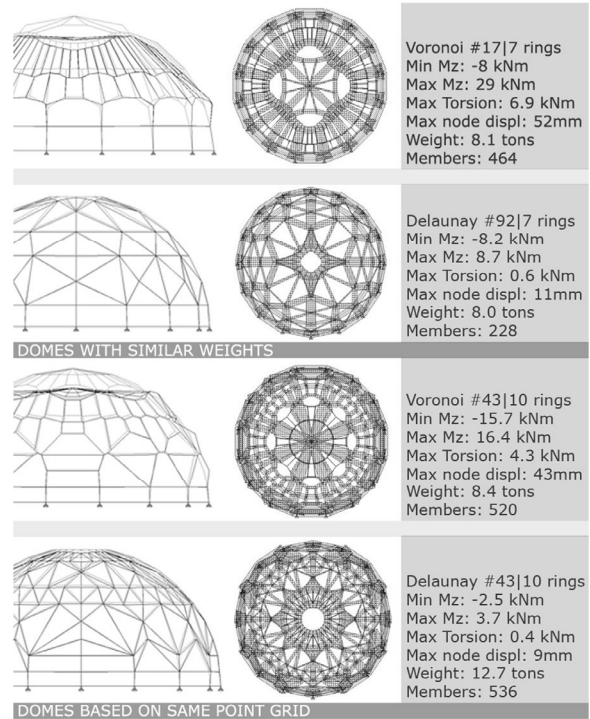
Delaunay Domes



## Examples (with Michela Turrin & Maria Van Embden Andres)

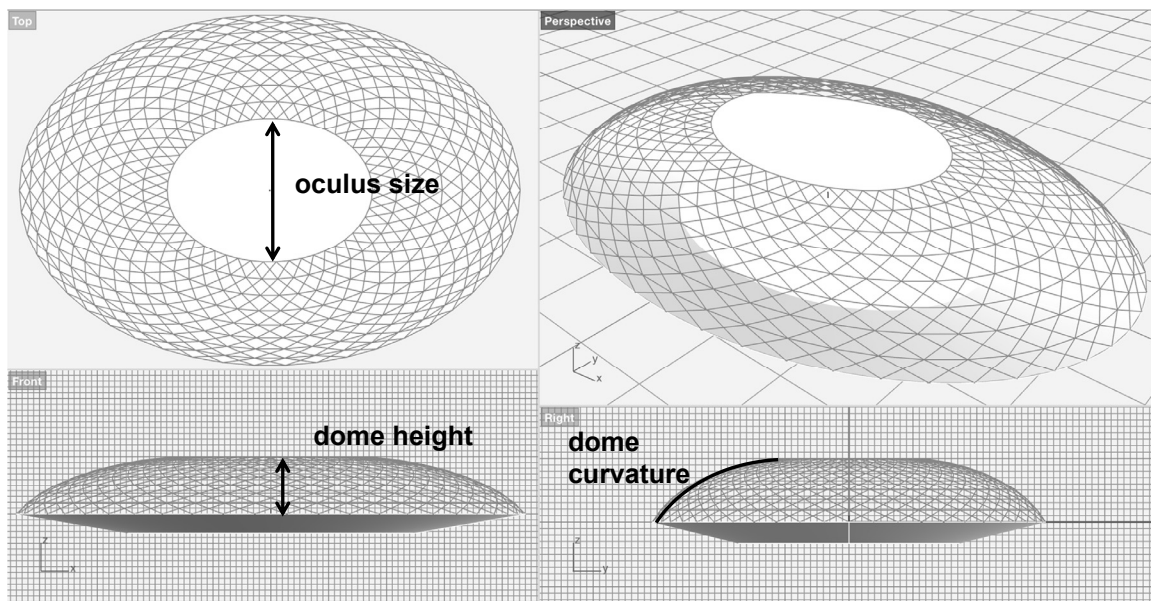


Geometry Generation



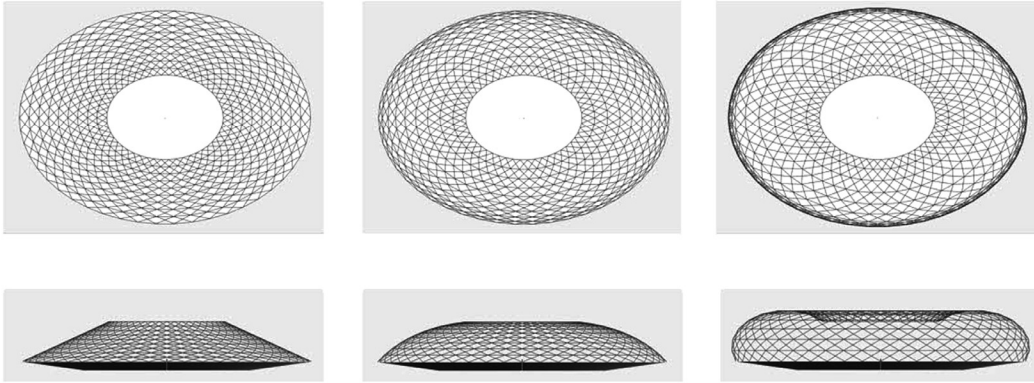
Structural Performance

## Examples (with Andre Chaszar) Soccer Stadium - variables

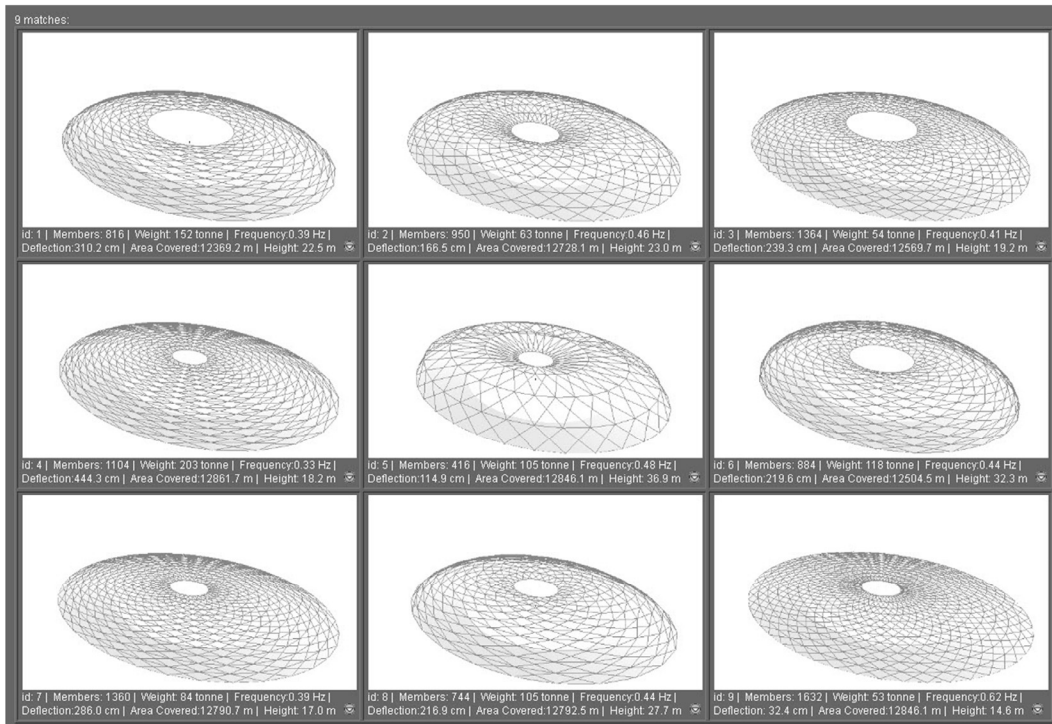


## Examples (with Andre Chaszar) Soccer Stadium - performance

- Geometry: curvature, oculus, mesh density, number of elements
- Structural: weight, deflection, modal frequency
- Daylighting: light intensity and distribution on field

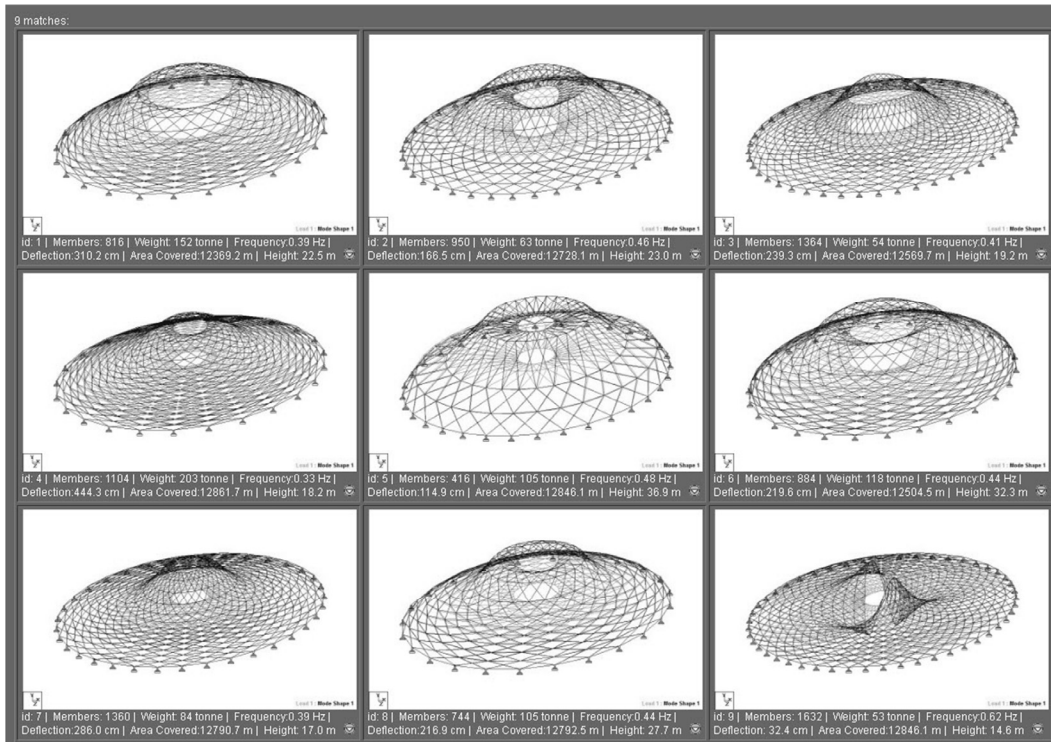


## Examples (with Andre Chaszar) Soccer Stadium - geometry





## Examples (with Andre Chaszar) Soccer Stadium - modal frequencies



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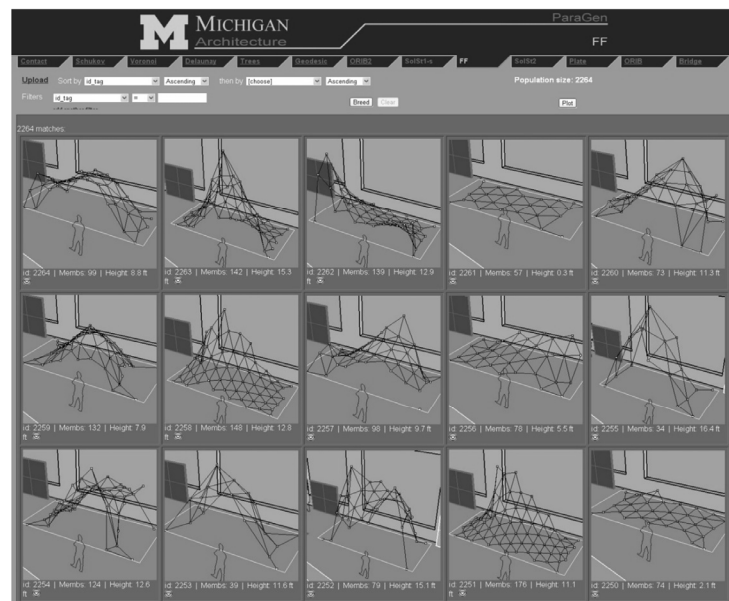
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## Examples Foam & Fabric M. with M. Wright & M. Jensen

Designer selected populations based on visual criteria.

Generated with a Python script in Rhino

Full solution set of 2200



Peter von Buelow

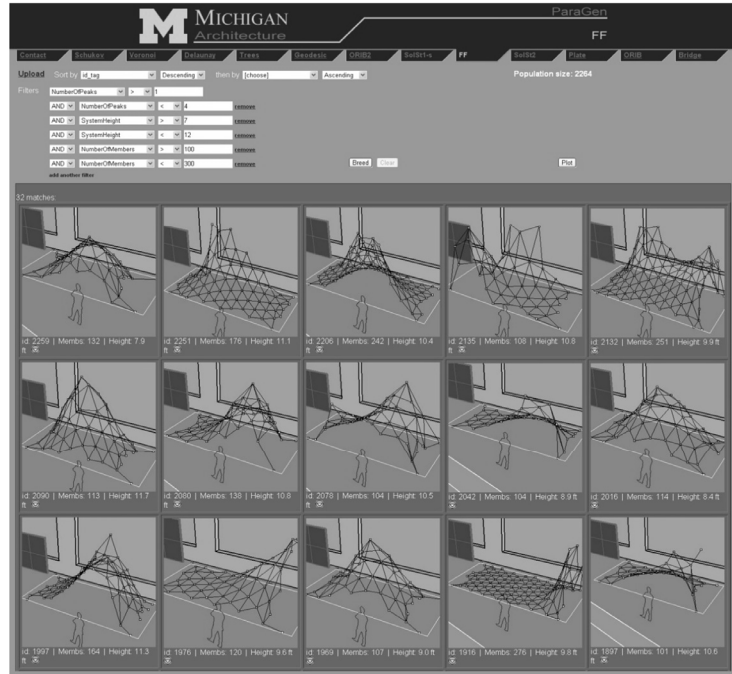
University of Michigan

Taubman College

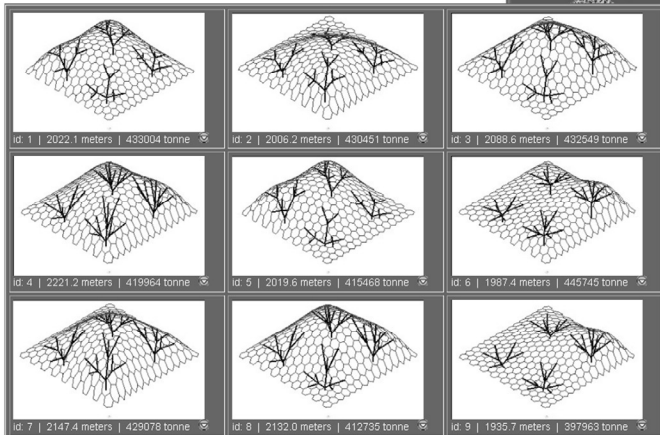
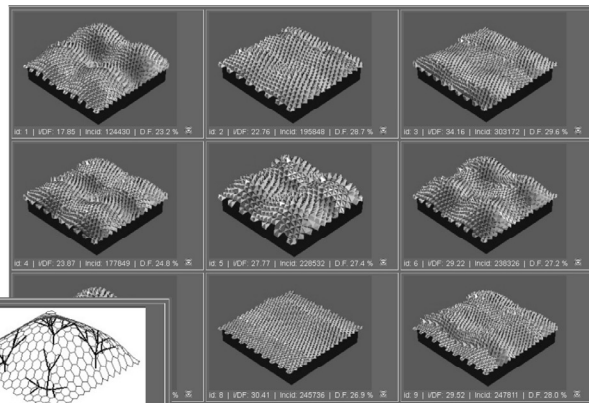
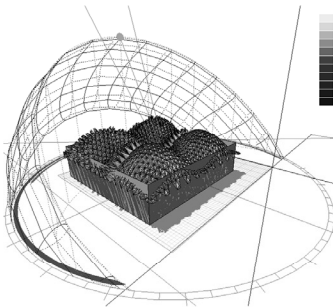
# Examples Foam & Fabric M. With M. Wright & M. Jensen

Post process  
 Post process  
 exploration with SQL  
 exploration with SQL  
 sorts and filters  
 sorts and filters

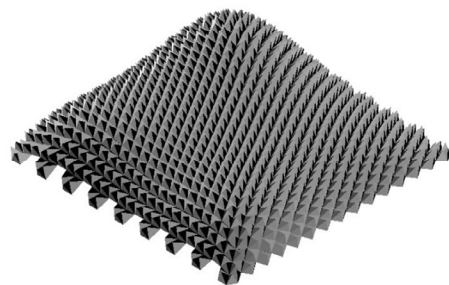
Reduced set of 32  
 Reduced set of 32



# Examples (with Michela Turrin & Andreas Falk) SoSt

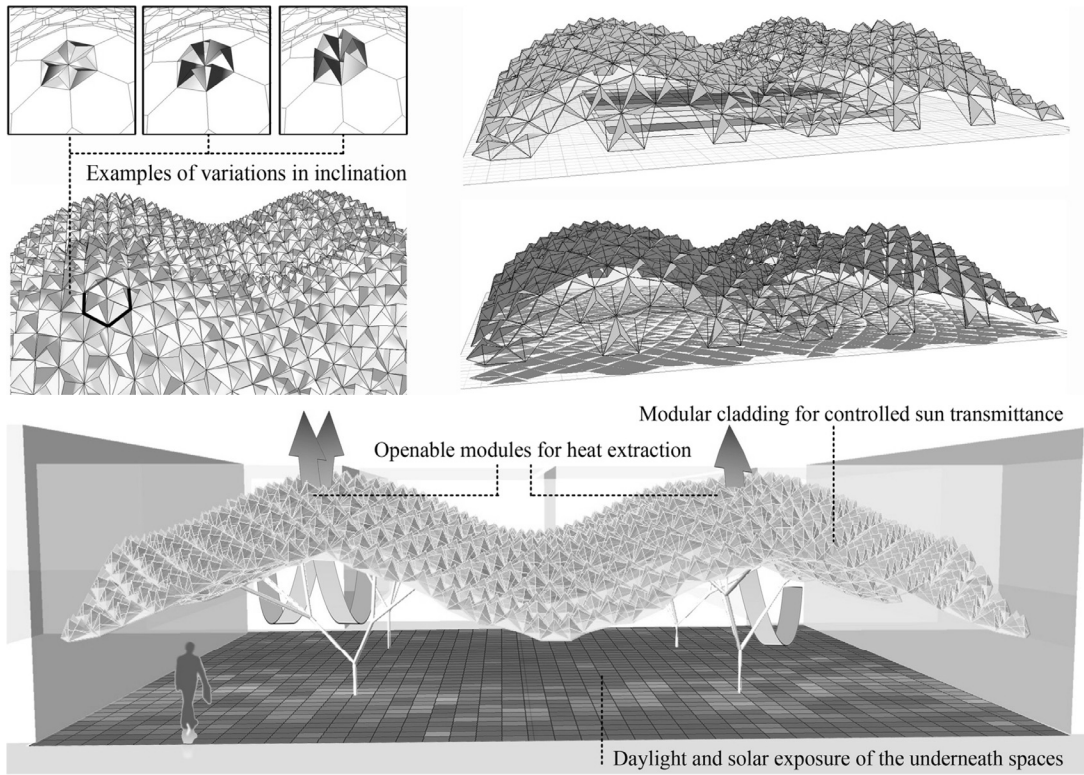


Shading / Ventilation

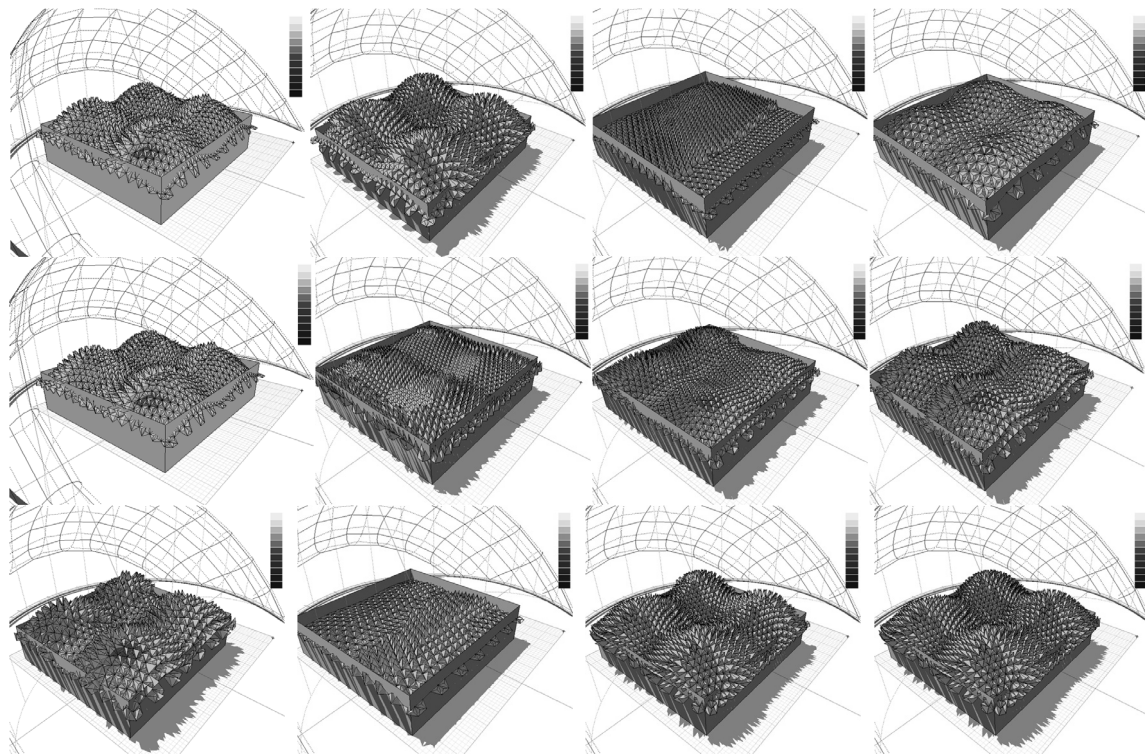


Branching Columns

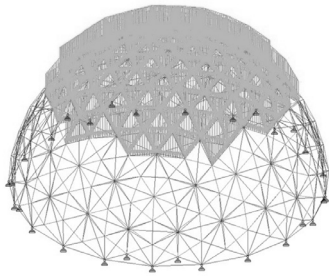
# Examples (with Michela Turrin & Andreas Falk) SoSt



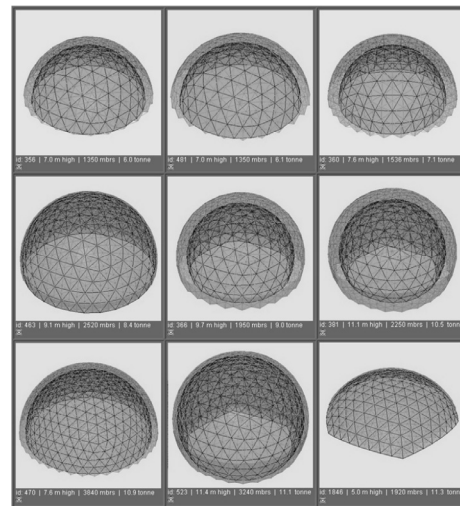
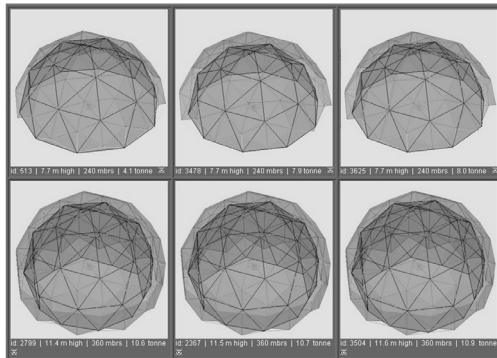
# Examples (with Michela Turrin & Andreas Falk) SoSt



## Examples – Geodesic Domes (with Ted Hall)



Snow Loading



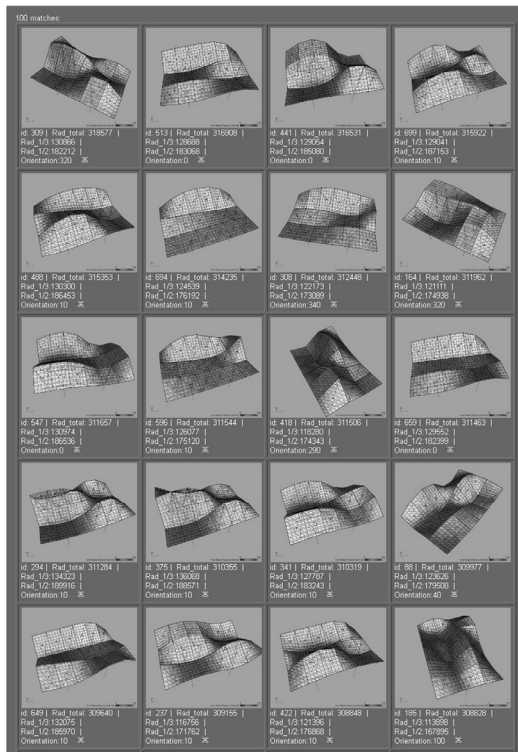
### Variable parameters

- Outer shell polyhedral type
- Power – subdivisions
- Frequency
- Base trim
- Distance between layers

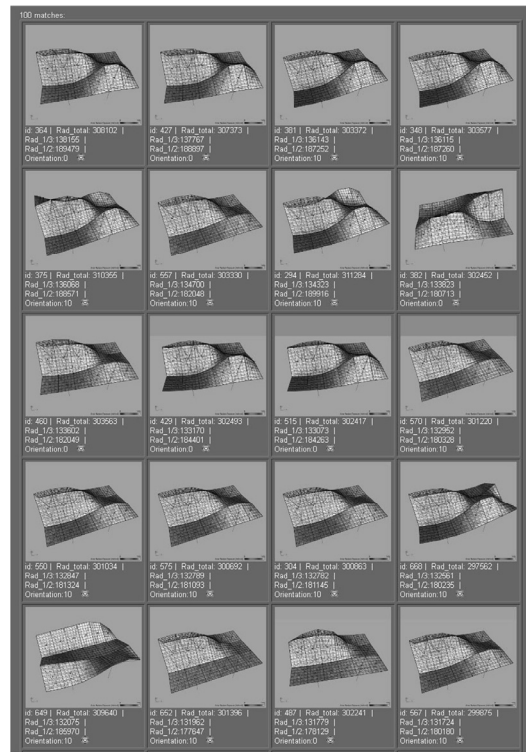
## Examples – NetZeroEnergy (with Studio [Ci] + Constance Bodurow)



## Examples – NetZeroEnergy (with Studio [Ci] + Constance Bodurow)



PV on all panels



PV on 6 panels

## Examples – LIMB (with Steven Mankouche & Kasey Vliet)

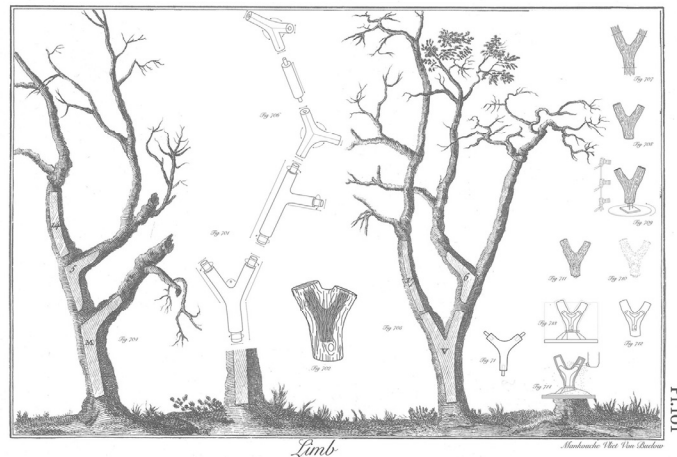
### Tree Crotch Joints

Used in 18th century ship building

Replaces mortise and tendon joint with a single element

Grain of wood follows the force path

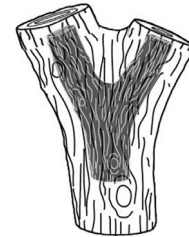
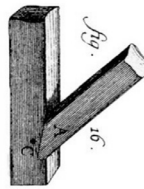
Can be milled to fit dimensions of a given structure



## Examples – LIMB (with Steven Mankouche & Kasey Vliet)

### Tree Crotch Joints

Final joints milled from the raw tree crotch



## Examples – LIMB (with Steven Mankouche & Kasey Vliet)

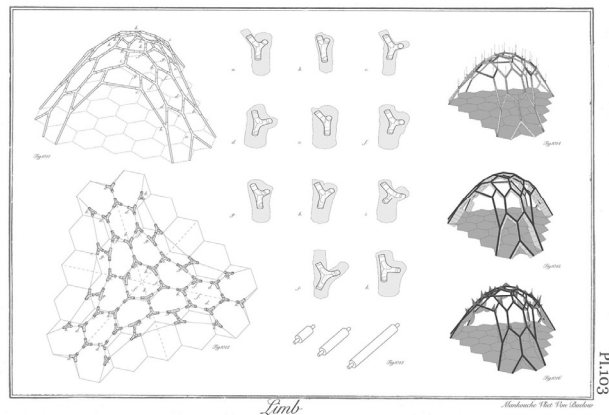
Based on hexagonal mesh

Joints connect 3 struts

Designed as a catenary vault

Form adjusted to fit given joints

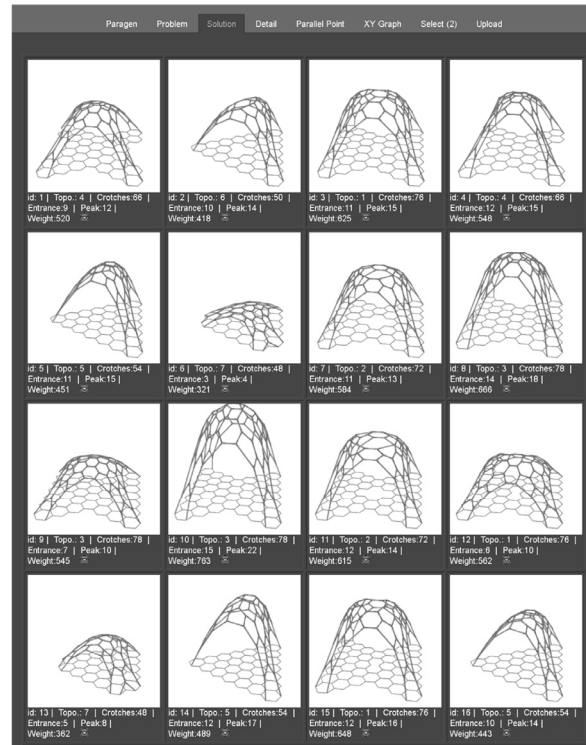
Parametric exploration of topology and geometry options using Rhino/Grasshopper with Kangaroo and Karamba



## Examples – LIMB (with Steven Mankouche & Kasey Vliet)

### Design Parameters

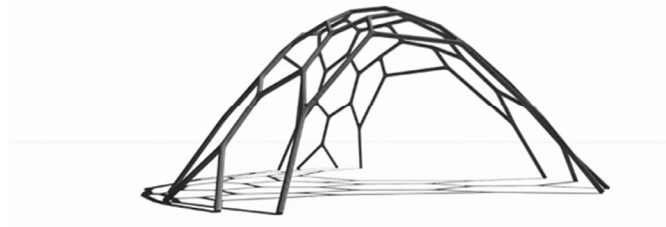
- Minimize out of plane curvature
- Naturally occurring bifurcation angles (30-90°)
- Axially aligned joints and connectors
- Minimize number of joints
- Smooth shell surface
- Entrance and center height
- Weight
- Member forces
- Deformation



## Examples – LIMB (with Steven Mankouche & Kasey Vliet)

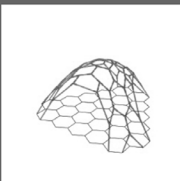





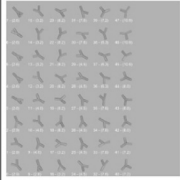
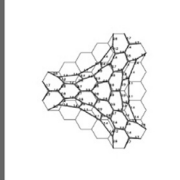
### Form Generation

- Using ParaGen exploration method with Grasshopper
- Each solution analyzed in Grasshopper
- Solutions saved with images in MySQL
- Initial generation ca. 500
- Breeding for:
  - entrance > 2 m (6.5 ft)
  - peak < 3 m (10 ft)
  - minimum joints



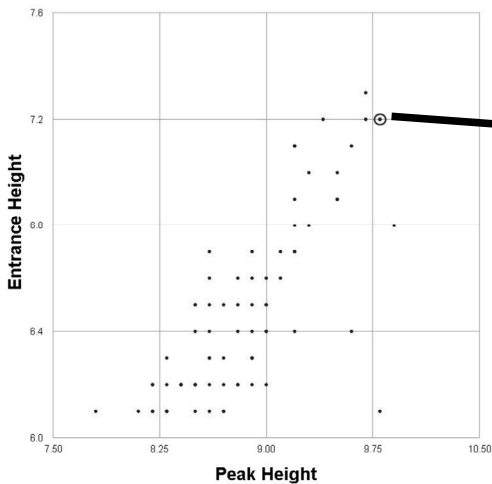
# Examples – LIMB (with Steven Mankouche & Kasey Vliet)



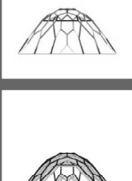
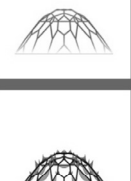

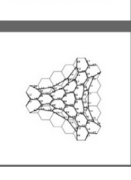
## Collected Data

ID number	241		
Dome Typology	7		
Branching Members Rest Length Ratio	0.4		
Boundry Members Rest Length Ratio	1		
Central Members Rest Length Ratio	0.4		
Upward Force	1.7		
Parent 1	0		
Parent 2	0		
Number of Crotches	48		
Number of Members	87		
Minimum Member Length	0.36 FT		
Maximum Member Length	2.64 FT		
Entrance Height	7.2 FT		
Peak Height	9.8 FT		
Dome Weight	395 LBS		
Displacemnt	0.012 IN		
Maximum Tensile Utilization	-2.3		
Maximum Compressive Utilization	7.1		
Minimum Crotch Angle	36 degrees		
Maximum Crotch Angle	167 degrees		
Min Crotch Out-of-Plane Angle	2.6 degrees		
Max Crotch Out-of-Plane Angle	10.9 degrees		
Machine IP	67.194.43.88		
Run Time	2018-06-20 14:42:32		

# Examples – LIMB (with Steven Mankouche & Kasey Vliet)

Peak Height vs. Entrance Height



ID number	241		
Dome Typology	7		
Branching Members Rest Length Ratio	0.4		
Boundry Members Rest Length Ratio	1		
Central Members Rest Length Ratio	0.4		
Upward Force	1.7		
Parent 1	0		
Parent 2	0		
Number of Crotches	48		
Number of Members	87		
Minimum Member Length	0.36 FT		
Maximum Member Length	2.64 FT		
Entrance Height	7.2 FT		
Peak Height	9.8 FT		
Dome Weight	395 LBS		
Displacemnt	0.012 IN		
Maximum Tensile Utilization	-2.3		
Maximum Compressive Utilization	7.1		
Minimum Crotch Angle	36 degrees		
Maximum Crotch Angle	167 degrees		
Min Crotch Out-of-Plane Angle	2.6 degrees		
Max Crotch Out-of-Plane Angle	10.9 degrees		
Machine IP	67.194.43.88		
Run Time	2018-06-20 14:42:32		



## Examples – LIMB (with Steven Mankouche & Kasey Vliet)



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## Examples – LIMB (with Steven Mankouche & Kasey Vliet)

### Constructed Prototype



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## Examples – LIMB (with Steven Mankouche & Kasey Vliet)

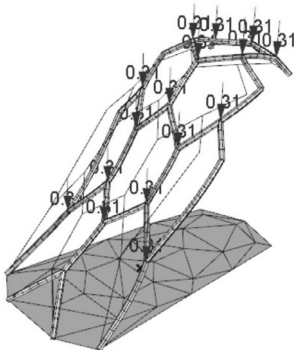
### Load Testing

- Load test to failure
- Hung sand buckets from nodes
- Deflection measurements on cards
- Maximum load: 311 N/node = 0.67kN/m<sup>2</sup>  
(70 lbs/node = 14 psf)
- Wood cracked at node



## Examples – LIMB (with Steven Mankouche & Kasey Vliet)

### Load Testing



## Examples – LIMB (with Steven Mankouche & Kasey Vliet)

### Load Testing

- Load test to failure
- Hung sand buckets from nodes
- Deflection measurements on cards
- Maximum load: 311 N/node = 0.67kN/m<sup>2</sup>  
(70 lbs/node = 14 psf)
- Wood cracked at node



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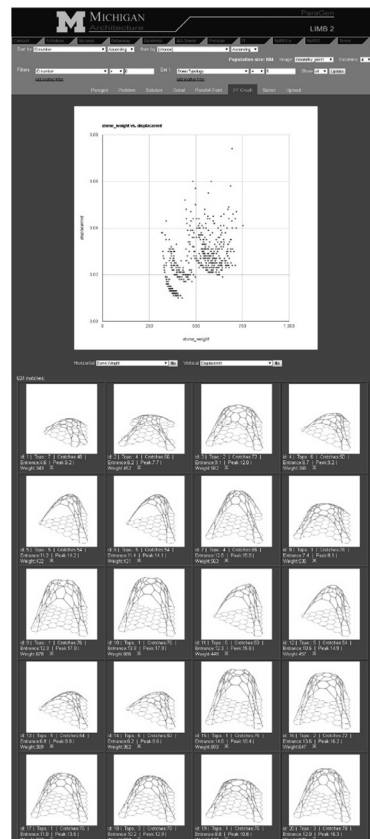
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## Genetically Enhanced Parametric Design for Performance Optimization and Design Exploration

Additional Information:

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[www.umich.edu/~pvbuelow](http://www.umich.edu/~pvbuelow)

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